

CSE 190 – Intro to Deep RL

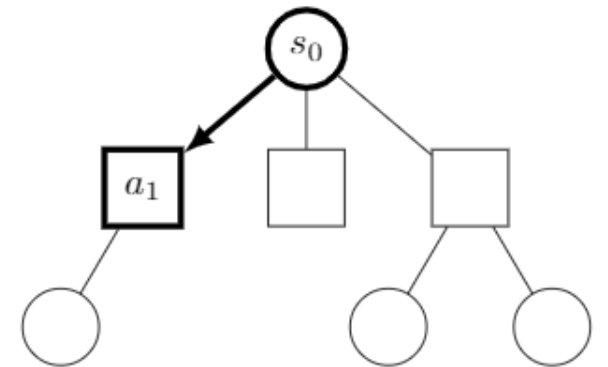
4/22 – Deep RL, pre-LLMs

Prithviraj Ammanabrolu

Thanks to David Silver's DeepMind RL Course and Rich Sutton's RL Book. Some slides were adapted from there.

Monte Carlo Tree Search

- 4 phases of building out and simulating paths along a search tree
- Various forms of this used in everything from Alpha Zero to modern LLM inference
- For arbitrary problem with start state s_0 and actions a_i
- All states have attributes:
 - Total simulation reward $Q(s)$ and
 - Total no. of visits $N(s)$



Why Reinforcement Learning?

- Reinforcement Learning:
 - The environment is initially unknown
 - The agent interacts with the environment
 - The agent improves its policy
- Planning:
 - A model of the environment is known
 - The agent performs computations with its model (without any external interaction)
 - The agent improves its policy a.k.a. deliberation, reasoning, introspection, pondering, thought, search

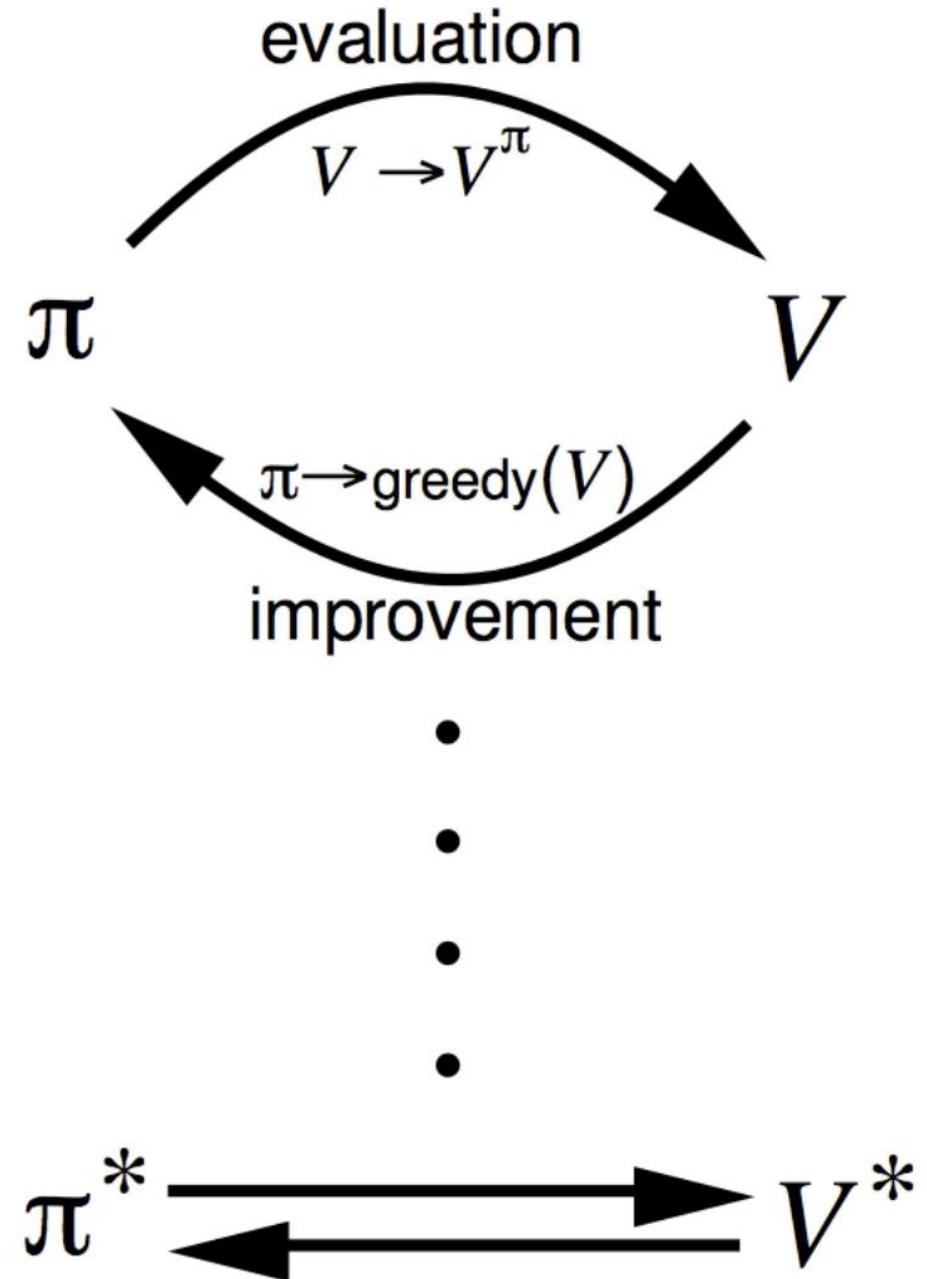
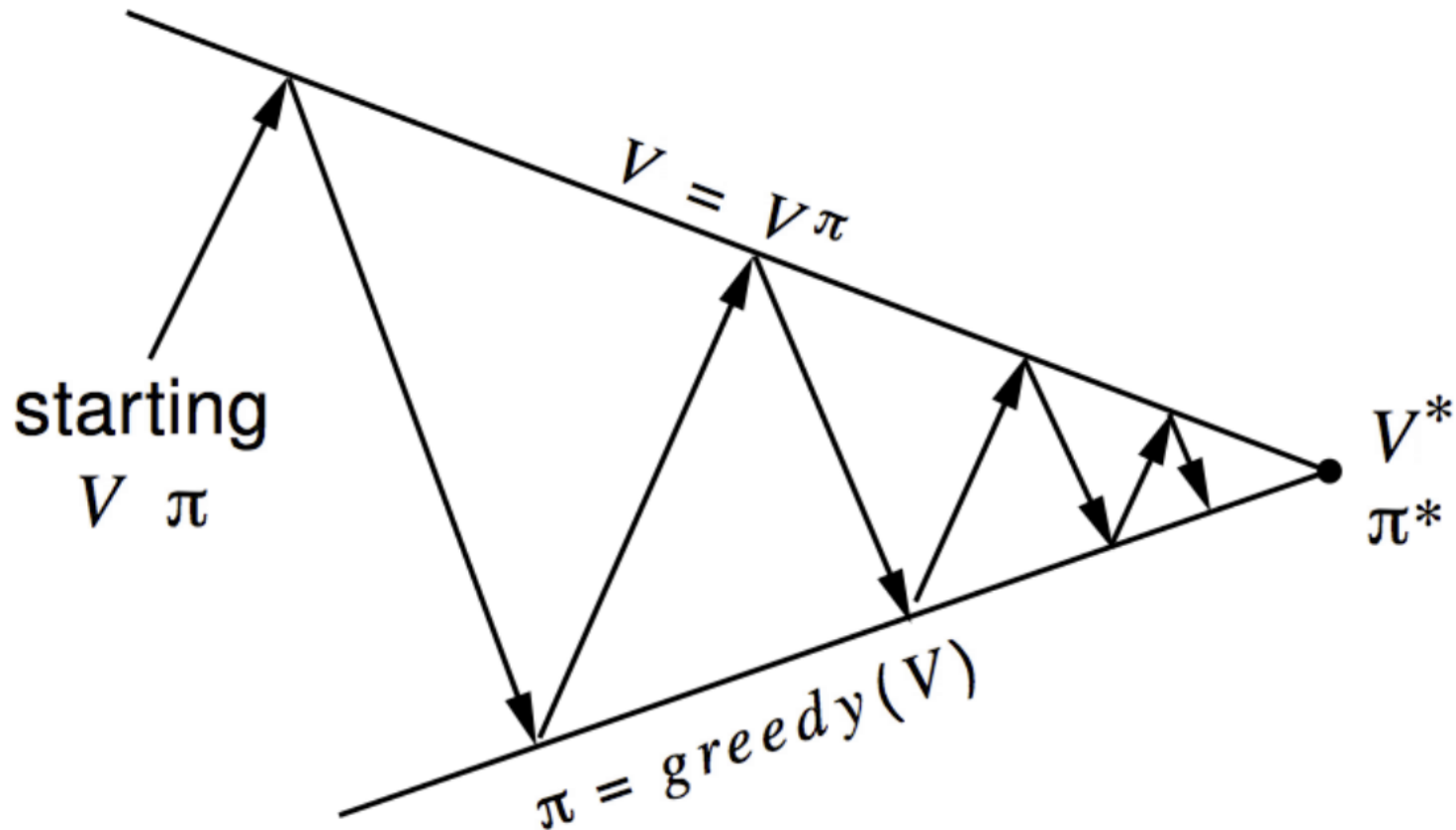
When to use DP

Dynamic Programming is a very general solution method for problems which have two properties:

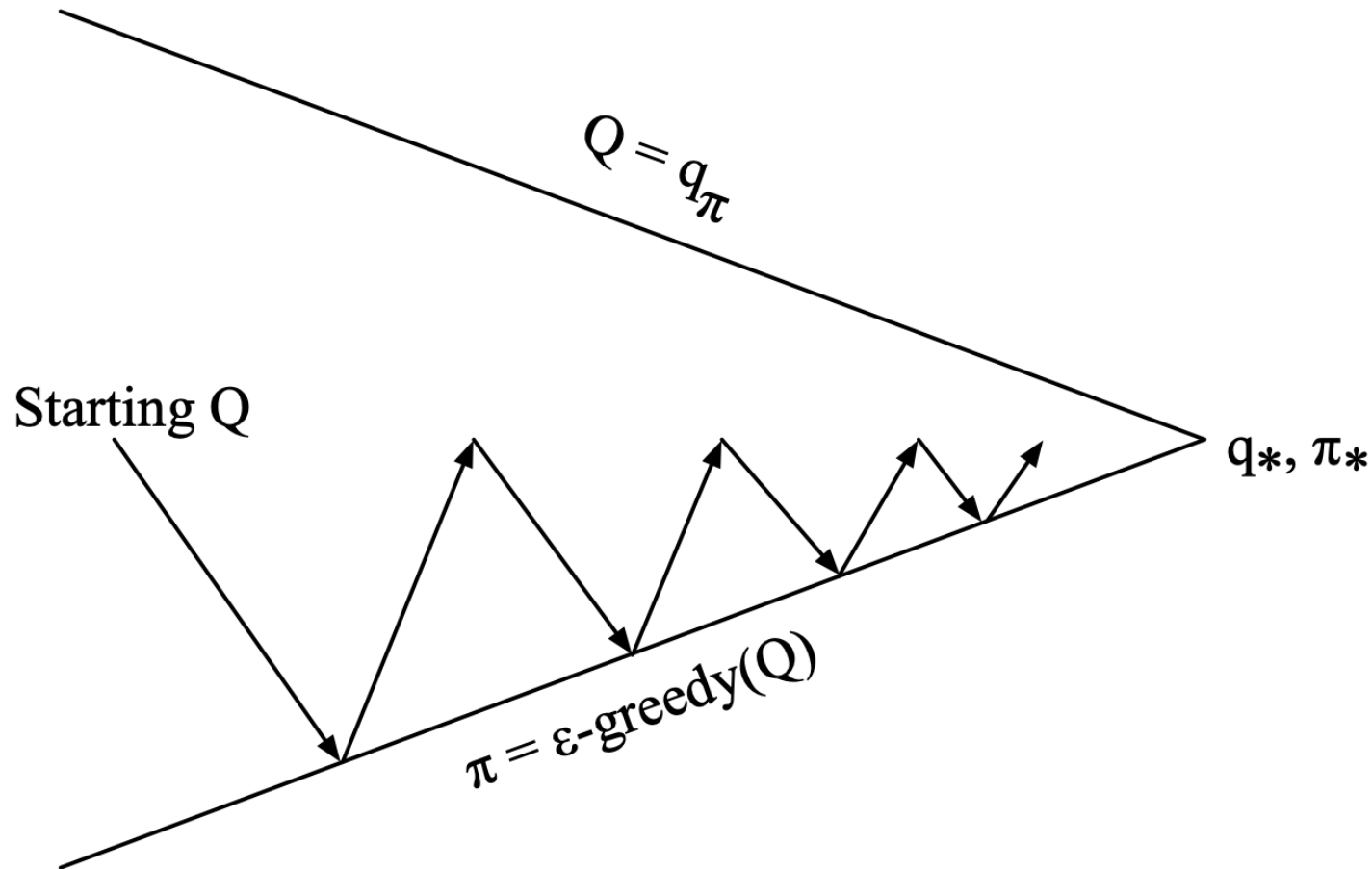
- Optimal substructure:
 - Principle of optimality applies
 - Optimal solution can be decomposed into subproblems
- Overlapping subproblems:
 - Subproblems recur many times
 - Solutions can be cached and reused
- Markov decision processes satisfy both properties Bellman equation gives recursive decomposition Value function stores and reuses solutions

Generalized Policy Iteration

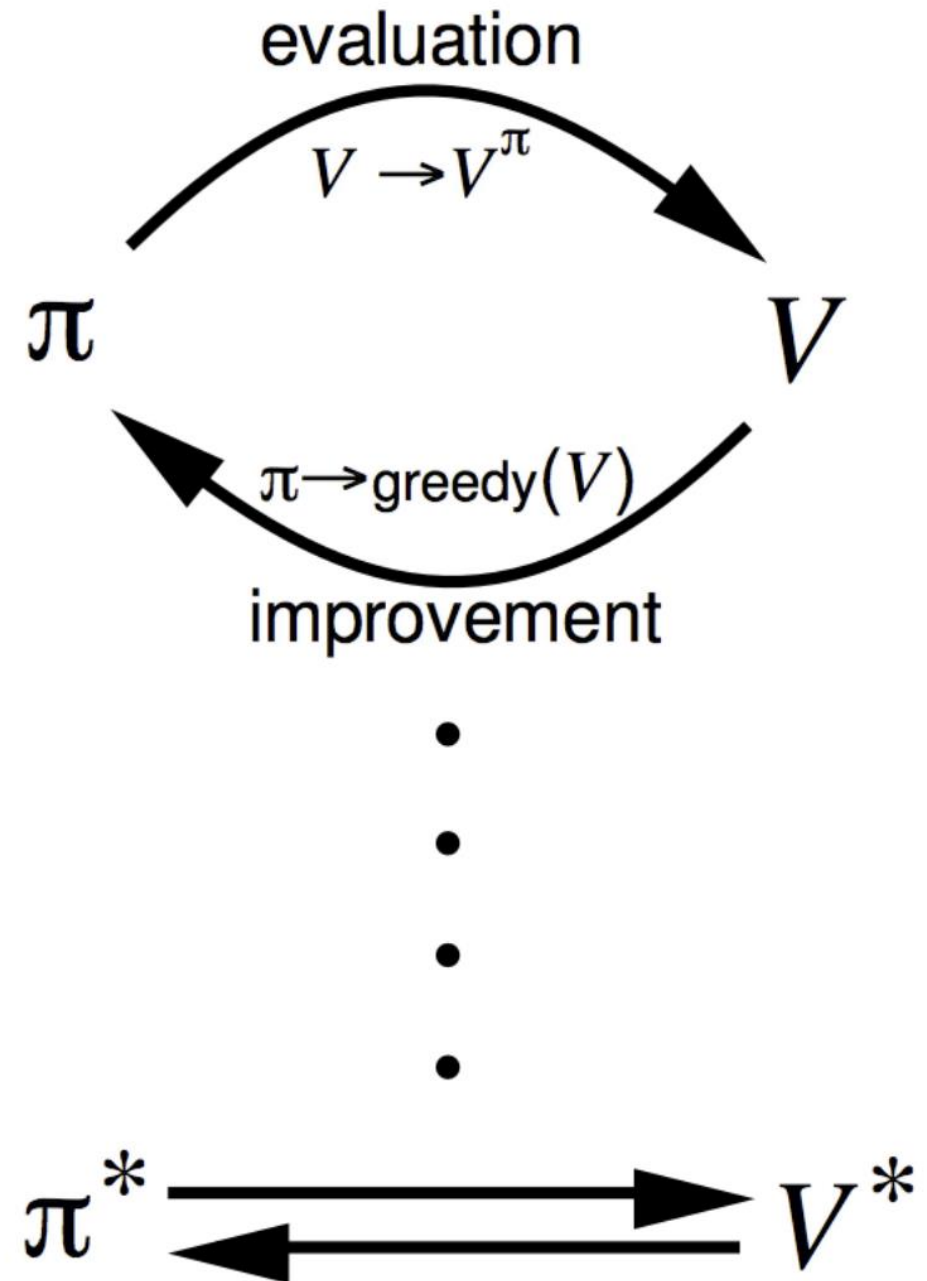
- Both are iterative versions of this



Generalized Policy Iteration with Fn Approximation + Monte Carlo Eval



You can't fully evaluate the entire state space each time



Issues with Monte Carlo estimates

- Need returns for whole trajectory
- The larger the state space is and the longer the horizon, the harder it is to get good estimates
- High variance, very dependent on “getting lucky” and seeing high return trajectories

How to fix? Temporal Difference

- With *Monte Carlo*, we update the value function from a complete episode, and so we **use the actual accurate discounted return of this episode**.

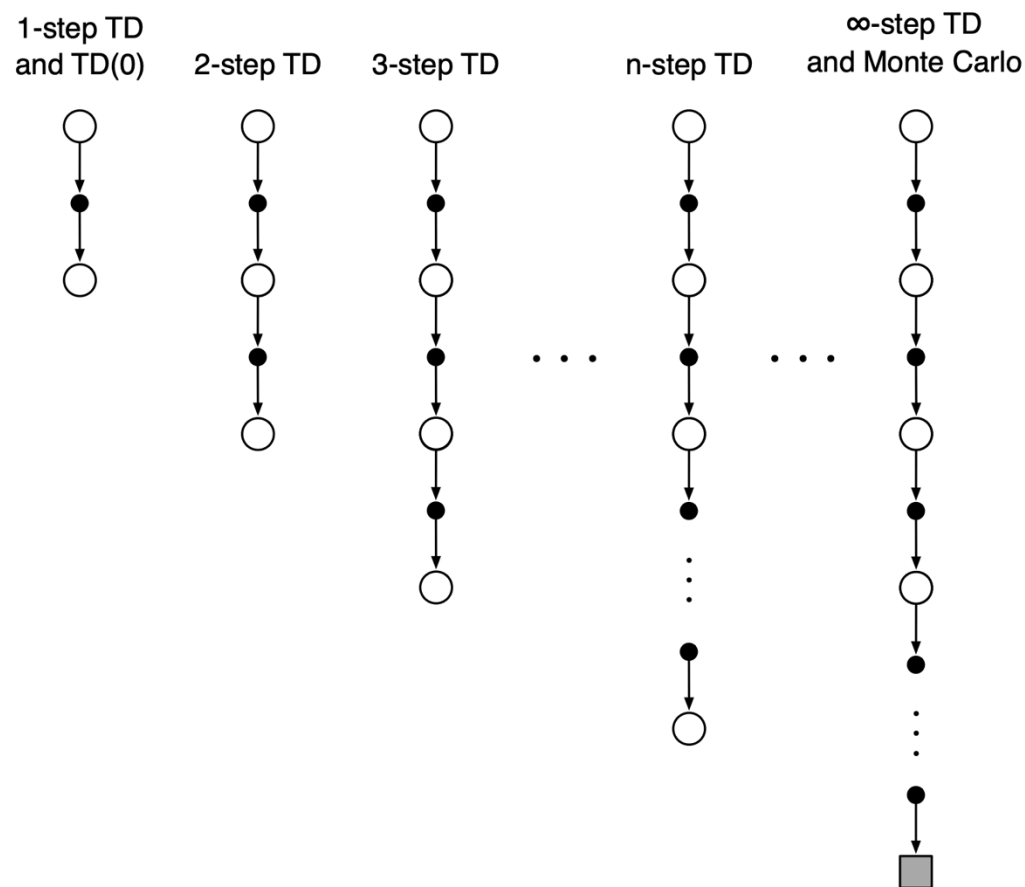
Monte Carlo: $V(S_t) \leftarrow V(S_t) + \alpha[G_t - V(S_t)]$

- With *TD Learning*, we update the value function from a step, and we replace G_t , which we don't know, with **an estimated return called the TD target – a bootstrapping method similar to DP**

TD Learning: $V(S_t) \leftarrow V(S_t) + \alpha[R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$

TD(0) \rightarrow TD(∞)

$$V(S_t) \leftarrow V(S_t) + \alpha[R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$$



TD Advantages

- Temporal-difference (TD) learning has several advantages over Monte-Carlo (MC)
 - Lower variance
 - Online
 - Incomplete sequences
- Natural idea: use TD instead of MC in our control loop Apply TD to $Q(S, A)$ Use ϵ -greedy policy improvement Update every time-step

TD Disadvantages

- Bootstrapping means you are chasing a moving target, stability of training very dependent on initialization

How to fix state space is very large

1. Learn from prior experiences
2. Function approximation

On Policy TD Learning - SARSA

- On Policy = learning the policy you are evaluating
- Will not cover SARSA as it is not really used anymore but will cover On Policy later on

Off-policy Learning

- Evaluate target policy $\pi(a|s)$ to compute $v_\pi(s)$ or $q_\pi(s, a)$
- While following behavior policy $\mu(a|s)$

$$\{S_1, A_1, R_2, \dots, S_T\} \sim \mu$$

Why is this important?

- Learn from observing humans or other agents
- Re-use experience generated from old policies $\pi_1, \pi_2, \dots, \pi_{t-1}$
- Learn about optimal policy while following exploratory policy
- Learn about multiple policies while following one policy

Q-Learning

- We now consider off-policy learning of action-values $Q(s, a)$
- Next action is chosen using behavior policy $A_{t+1} \sim \mu(\cdot|S_t)$
- But we consider alternative successor action $A' \sim \pi(\cdot|S_t)$
- And update $Q(S_t, A_t)$ towards value of alternative action from policy you're actually evaluating

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha R_{t+1} + \gamma Q(S_{t+1}, A') - Q(S_t, A_t)$$

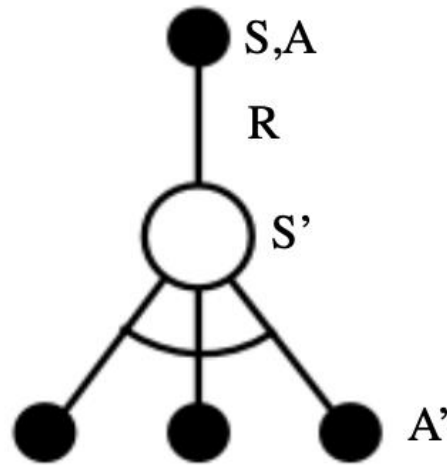
Q-Learning

- We now allow both behavior and target policies to improve
- The target policy π is greedy w.r.t. $Q(s, a)$
- $\pi(S_{t+1}) = \operatorname{argmax}_a Q(S_{t+1}, a')$
- The behavior policy μ is e.g. ϵ -greedy w.r.t. $Q(s, a)$
- The Q-learning target then simplifies:

$$\begin{aligned} & R_{t+1} + \gamma Q(S_{t+1}, A_t) \\ &= R_{t+1} + \gamma Q(S_{t+1}, \operatorname{argmax}_a Q(S_{t+1}, a')) \\ &= R_{t+1} + \max_a \gamma Q(S_{t+1}, a') \end{aligned}$$

Q-Learning

- $Q(S, A) \leftarrow Q(S, A) + \alpha (R + \gamma \max_{a'} Q(S', a') - Q(S, A))$
- Q-learning control converges to the optimal action-value function, $Q(s, a) \rightarrow q^*(s, a)$



Q-Learning Full Algorithm

Initialize $Q(s, a), \forall s \in \mathcal{S}, a \in \mathcal{A}(s)$, arbitrarily, and $Q(\text{terminal-state}, \cdot) = 0$
Repeat (for each episode):
 Initialize S
 Repeat (for each step of episode):
 Choose A from S using policy derived from Q (e.g., ϵ -greedy)
 Take action A , observe R, S'
 $Q(S, A) \leftarrow Q(S, A) + \alpha [R + \gamma \max_a Q(S', a) - Q(S, A)]$
 $S \leftarrow S'$
 until S is terminal

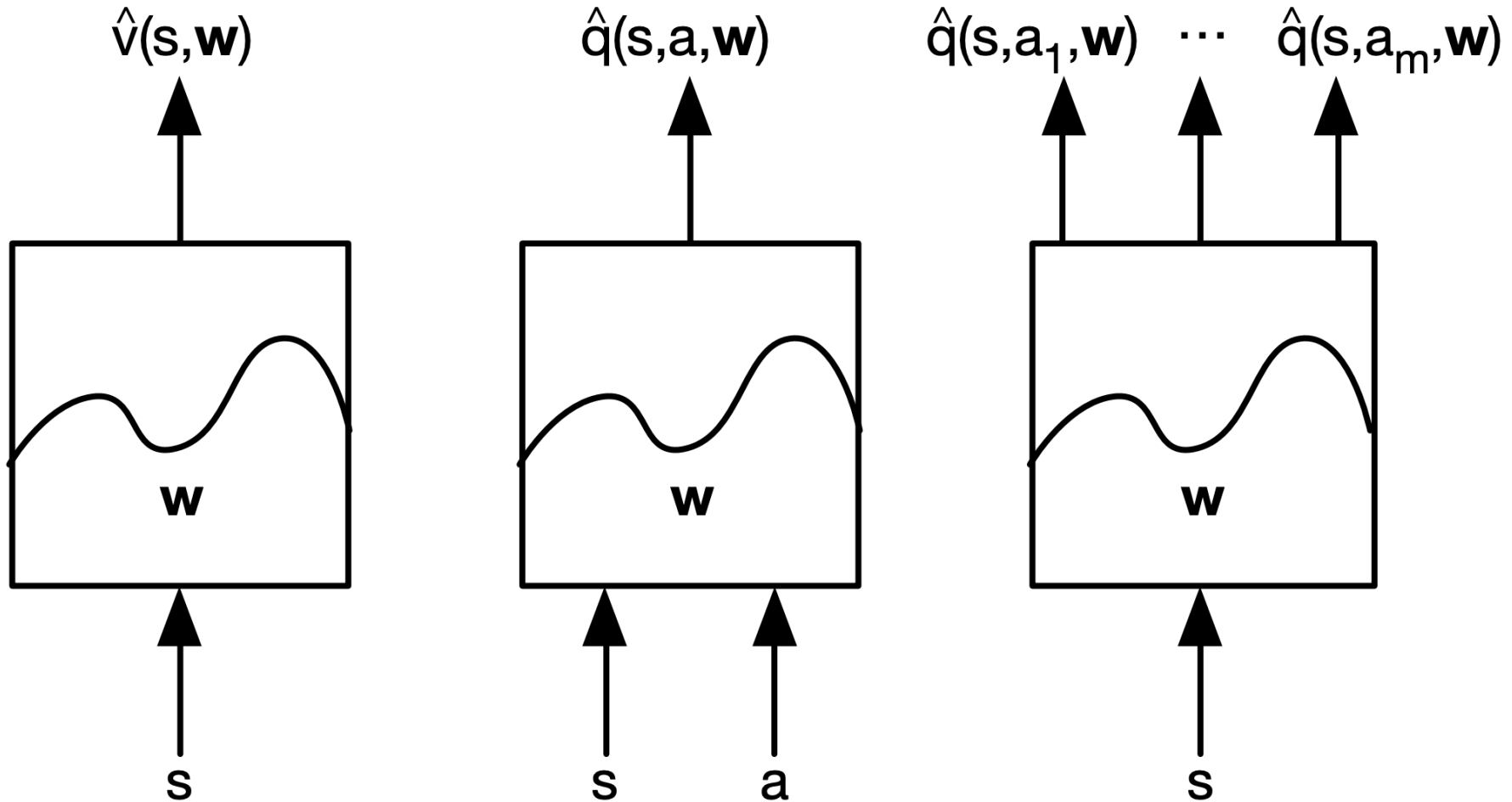
Kinda Large Scale RL

- Reinforcement learning can be used to solve large problems, e.g.
 - Backgammon: 10^{20} states
 - Computer Go: 10^{170} states
 - Helicopter: continuous state space
- How can we scale up the model-free methods for prediction and control from the last two lectures?

Value Function Approximation

- So far we have represented value function by a lookup table
- Every state s has an entry $V(s)$
- Or every state-action pair s, a has an entry $Q(s, a)$
- Problem with large MDPs:
 - There are too many states and/or actions to store in memory
 - It is too slow to learn the value of each state individually
- Solution for large MDPs:
 - Estimate value function with function approximation
$$\hat{v}(s, w) \approx v_{\pi}(s) \text{ or } \hat{q}(s, a, w) \approx q_{\pi}(s, a)$$
 - Generalize from seen states to unseen states
 - Update parameter w using MC or TD learning

Types of Value Function Approximators



Action-value Function Approximation

- Approximate the action-value function

$$\hat{q}(S, A, w) \approx q_{\pi}(S, A)$$

- Minimize mean-squared error between approximate action-value fn $\hat{q}(S, A, w)$ and true action-value fn $q_{\pi}(S, A)$

$$J(w) = E_{\pi} [(q_{\pi}(S, A) - \hat{q}(S, A, w))^2]$$

- Use stochastic gradient descent to find a local minimum

$$- 1/2 \nabla_w J(w) = (q_{\pi}(S, A) - \hat{q}(S, A, w)) \nabla_w \hat{q}(S, A, w)$$

$$\Delta w = \alpha (q_{\pi}(S, A) - \hat{q}(S, A, w)) \nabla_w \hat{q}(S, A, w)$$

Deep Neural Nets as function approx.

- Need a Neural Net that is actually able to effectively encode observations and actions
- For the original Atari, this was CNNs
- These days, it is transformers
- Note that you generally need hundreds of k to millions of steps for most environments. The bigger your policy the slower this is

Deep Q Network - DQN

- You actually know all the pieces now
- You put Q-learning together with the function approximation

General loop

Algorithm 1 Deep Q-learning with Experience Replay

Initialize replay memory \mathcal{D} to capacity N

Initialize action-value function Q with random weights

for episode = 1, M **do**

 Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$

for $t = 1, T$ **do**

 With probability ϵ select a random action a_t

 otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$

 Execute action a_t in emulator and observe reward r_t and image x_{t+1}

 Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$

 Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D}

 Sample random minibatch of transitions $(\phi_j, a_j, r_j, \phi_{j+1})$ from \mathcal{D}

 Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$

 Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3

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end for

end for

Where are we now?

- GPU go brrrr as solution to large state space RL
- Algorithms still not particularly efficient
- No guarantees on anything